

Application of Queuing Theory to Optimize Waiting-Time in Hospital Operations

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ABSTRACT

Waiting time is inherent to the healthcare service sector in India and a major challenge faced by almost every big hospital is queuing. Long waiting time can be a reflection of inefficiency in hospital operations. The out-patient department (OPD) has the biggest queue as compared to other departments in hospital operations. This study comprises of in-depth analysis of OPD from different dimensions. Like in many big hospitals across India, the OPD of Fortis Escorts Hospital in Jaipur, India is managed using experience and rule of thumb rather than strategic research-based techniques such as queuing theory. The Fortis Escorts Hospital in Jaipur receives a large number of patients each day which results in longer waiting time for patients due to long queues. To address this challenge, a SWOT analysis was conducted for the OPD of Fortis Escorts Hospital Jaipur (FEHJ) which resulted into dissecting the queuing problem and coming out with solutions knowing where the hospital operations can excel and where there is a scope of improvement to make the working and processes better. Additionally, after examining the problem analytically and applying queuing theory, measures were suggested to improve the delay points and make the OPD more efficient in order to gain a high patient satisfaction rating.

Keywords: queuing theory, OPD, waiting time, hospital operations, SWOT, patient satisfaction

1. INTRODUCTION

Hospital services operations particularly, the outpatient department plays a crucial role in providing quality healthcare for multi-specialty hospitals (Carman, 1990). The outpatient department (OPD) often acts as a profit centre in hospital operations not only for investing in new technology but also to curb losses on inpatient services (Green, 2006). However, despite the importance of OPD, hospitals fail to address complaints regarding long waiting time caused majorly due to observable queues which result in patient dissatisfaction (Kim *et al.*, 2009). Thus, hospital service operations should have a smooth flow to satisfy the patient's

expectations by redesigning their systems and adapting to the best practices and tools with improved processes (Natarajan, 2006) which has a huge scope in developing economies such as India (Natchair *et al.*, 1994).

The OPD of a hospital acts as a bridge between hospital and community, hence it is very important to plan the OPD with the idea of maximizing the utilization and quick turnover. (McQuarrie, 1983). It is imperative to have effective co-operation between the medical services and the support line services catering to the OPD requirements (Kritchanchai, 2012). The interpersonal skills of the medical personnel, availability of medicine, hospital infrastructure and medical information plays an important role in managing OPD and create a positive influence on patient satisfaction (Natarajan, 2006). Hence, it is necessary to focus on optimizing waiting time in hospital operations for the benefit and wellbeing of patients.

Due to poor hospital service operations, patients tend to spend a lot of time getting the services they need (Dellaert *et al.*, 2015; Lohlun *et al.*, 2015). Long queues are an indication of lack of coordination, poor management, and insufficient resources, which affects the quality of services in hospital operations and reduce patients' satisfaction (Basta *et al.*, 2016; Bringedal, 2016; Bachmann and Barron, 1997). Given the role of waiting time in improving service quality for the higher satisfaction of patients, it is necessary to review it as one of the most common problems in hospital service operations (Benson *et al.*, 2001; Bleustein *et al.*, 2014).

Application of queuing theory for analysis and modeling of processes that involves waiting lines is used widely in industries for optimizing the supply of fixed resources at variable demand conditions, however, the healthcare industry views itself differently from other industry (Kritchanchai, 2012). The hospital operations managers should be aware of the status of business processes to improve operational performances and reduce the waiting time (Hall *et al.*, 2006). There are several analytical tools for understanding the complexity of a system's performance,

among which the queuing theory is a tool to analyze systems which include queues and consist of clients, servers, and queues (Kay *et al.*, 1996; Van Wyk and Walubo, 2014). Queuing theory is a scientific approach to minimize system inefficiencies and increase the patients' satisfaction (Bahadori *et al.*, 2014; Mayhew and Smith, 2008). The hospital operations managers can increase patients' satisfaction by making the right decisions through a proper understanding of the queuing theory and variables related to the patients' waiting time (Komashie *et al.*, 2015).

There is a lot of research available on queuing analysis related to a variety of hospital services such as cardiac care units, operating rooms, and emergency services. However, due to a lack of real-world validation, many proposed queuing models have yet to be adopted by hospital authorities. Therefore, there is a need to explore the utility and implications of queuing theory by validating a simple queuing model in a busy hospital of India. This paper through an actual OPD study of a large multi-specialty hospital shows how improvements in out-patient flow through streamlining of OPD processes can be achieved using SWOT analysis and queuing model. The study was conducted in a multi-specialty hospital called Fortis Escorts Hospital, Jaipur (FEHJ) which is a NABH accredited hospital with 250 beds and spread over an area of 3.67 acres in the capital of one of the largest states in India. Due to a wide variety of healthcare services provided by FEHJ, it took a long time for patients arriving at OPD to meet the concerned specialist leading to the formation of the queue. Naturally, one of the major grievances among the majority of the patients was the time they spend while waiting in OPD. The key aim of the paper is to aid hospital service operations at FEHJ in identifying bottlenecks in service operations and potential areas for improvement in the system, with the objective of optimizing patients waiting time, thereby allowing a higher flow of patients in OPD using queuing model.

The flow of the paper is organized in terms of objectives which are as follows. First, the complete process flow of the OPD is studied which is our first objective. It is followed by SWOT analysis to identify areas where time is consumed making it second objective. The third objective is to understand how patients perceive waiting time through survey method. Then, we conduct time study in different OPD's as part of the fourth objective and lastly, using queuing model, we calculate the waiting time in different OPD's. Finally, based upon results obtained, we draw some conclusions and discuss some implications of our findings along with the limitations of the study.

2. LITERATURE REVIEW

There have been studies on waiting time in hospital operations focused on the doctor and patient consultations in general hospitals (Park, 2001) which found that the factors influencing waiting time were characteristics of healthcare providers, consultation and patient's characteristics (Hwang, 2006). The classification of studies on applying queuing theory to healthcare service can be based upon waiting time and utilization analysis (Yeo *et al.*, 2014), which can be further classified into those on renegeing (Broyles and Cochran, 2007), variable arrival rate (Worthington, 1987), priority queuing discipline (Fiems *et al.*, 2005) and blocking

(Koizumi *et al.*, 2005); whereas studies on system design with respect to queuing (Green *et al.*, 2006; Park and Kwag, 2009) are classified into cost minimization (Gorunescu *et al.*, 2002) and blocking. Based on size of the system (Hall *et al.*, 2013), studies have been conducted at department-level which includes Departments of Internal Medicine (Hwang, 2006), Orthopaedics (Yeo *et al.*, 2014), Emergency Room (Kim *et al.*, 2009; Mandelbaum *et al.*, 2012), Radiology (Park and Kwag, 2009) and MRI (Green and Savin, 2008); while those conducted at healthcare center-level had the whole outpatient department (Park, 2001; Ko, 2010; Kim *et al.*, 2008).

The analysis of waiting time in healthcare systems can be approached mathematically using queuing theory (Ozcan, 2006). It is been established that queuing theory can be used for improving patient waiting time in hospital operations by an extensive review of the literature (Green, 2006a; mcquarrie, 1983; Siddhartan *et al.*, 1996). There is already large publication involving the application of queuing theory to service operations in hospital settings (Adele and Barry, 2005; Ivalis and Millard, 2003; Vasanaawala *et al.*, 2005). Unfortunately, this vital tool is underutilized in most hospital operations across India. There has also been extensive research on queuing analysis to enhance performance at various hospital departments (Green, 2002; Kim *et al.*, 1999) and emergency departments (Green *et al.*, 2006). Most hospital operations involve appointment system and the use of queuing is done in either of the two ways i.e. First-in-first-out or different classes of patients solely based on priority for e.g. In case of an emergency which automatically gets first priority before others (Adele and Barry, 2005). It is indeed possible to optimize patient waiting time on a priority basis by addressing the issue of which patient requires shorter service time (mcquarrie, 1983). The studies on models of queuing theory are provided by Green (2006a) and analysis of the effect of waiting times on patients in the Emergency Department is given by (Siddhartan *et al.*, 1996). The flow of patients in a queue can lead to good patient flow if the queuing is minimized whereas queuing delays can lead to patient suffering causing poor patient flow (Hall *et al.*, 2006). The demand for health care services can be determined by effective resource allocation and capacity planning (Murray, 2000). Based on specific probability assumptions, queuing theory can be used to provide an exact or approximate estimate of performance measures (Daulatani *et al.*, 2016). However, the results are approximated because the assumptions rarely hold (Cochran *et al.*, 2006).

Lewis, Bernard & Booms (1983) have defined that service quality is a measure of the gap between customer expectations and perceptions, and meeting customer expectations on a consistent basis. The outcome of the evaluation process is defined as perceived service quality and consumers tend to compare his expectations with the services received (Gronroos, 1984). Parasuraman *et al.*, (1991) emphasized the use of SERVQUAL as a diagnostic methodology for addressing service quality shortfalls and strengths. SERVQUAL has been extensively used to measure service quality in a variety of service sectors such as healthcare (Carman, 1990; Kilbourne *et al.*, 2004). Service quality focuses on meeting customers' needs and requirement and how well the delivered service meets the expectations of customers (Lewis and Booms, 1983). Customer dissatisfaction occurs when expectations are a higher and

perceived quality of service is less than satisfactory (Parasuraman *et al.*, 1988; Lewis and Mitchell, 1990).

Effective external communication creates realistic consumer expectations and enhances consumer perceptions which offset other service quality problems as well (Parasuraman *et al.*, 1985). Making patients entering OPD systems aware of the apparent services could improve service quality perceptions and increase awareness about hospital service operations (Kilbourne *et al.*, 2004). Patients are likely to perceive service delivered in a favorable way by segmenting on the basis of their service quality expectations which will ultimately lead to higher customer satisfaction. (Lewis *et al.*, 1990)

External communications affect not only consumer expectations about a service but also consumer's perceptions of the delivered service (Siddharta, 1996). Consumers' quality perceptions of the service quality model are influenced by a series of distinct gaps occurring on the marketer's side (Itumalla *et al.*, 2014). A key challenge for researchers is to devise methods to measure these gaps accurately (Parasuraman *et al.*, 1985). This paper intends to address the gap between actual service delivery and external communication about the hospital which affects service quality from a patient's point of view.

3. RESEARCH DESIGN

In service operations management, it is always recommended to use a standard methodology that enables to understand the current processes, determine the desired changes and improve them. The present paper aims at optimizing the performance of OPD department using queueing theory and increase patients' satisfaction. Using in-depth analysis of OPDs from different dimensions, the objectives involved in the study are listed as follows:

1. To study the complete process flow of the OPD at Fortis Escorts Hospital, Jaipur.
2. To identify areas where a patient's time is consumed by performing a SWOT analysis of the existing OPD.
3. To find out patient's perception of delay in OPD through a satisfaction survey.
4. To do time study on different OPD stations at Fortis Escorts Hospital, Jaipur.
5. To calculate the waiting time of patients in different OPD stations using queueing model.

4. RESEARCH METHODOLOGY

The management of patient flow is an important element in improving the efficiency of hospital service operations. It requires handling the arrival of patients, service process and queueing process, which directly impacts the delivery of healthcare services. Since it is a study which emphasizes the legal phenomenon of cause and effect of a condition, it is a positivist social science research done by cautiously using the empirical observations. The research methodology used in this paper is a case study due to the in-depth examination of an extensive amount of information

about very few units or cases across a single time frame. To optimize waiting time in hospital operations using queueing theory, the study design is a time study. The study was stretched around a week of observation for the OPD working pattern and the probable delay points, data collection of time consumed at each step involved in getting a consultation done in the OPD. The instrument used for the analysis was questionnaire and time study analysis were done for getting the results of the survey.

The study was conducted in two dimensions namely, Objective and the Subjective approach. In objective assessment, it was observed that for how much time the patients waited in the queue, the time they spent at the registration counter, the time consumed in reaching the OPD and the waiting time in the OPDs for consultation, etc. The initial part of the objective assessment involved identifying the key informant in OPD to get information about a general overview of the outpatient system. After that, the collection of more data and information related to this study was analyzed using a queueing model to optimize the waiting time and arrival pattern of the outpatient department for objective assessment. This data was then used for analyzing the situation and derive an insight to give recommendations which could reduce the waiting time for patients. The subjective approach included the patients' perception about the delay, the reasons behind the delay, the psychology and opinion regarding the promptness in the registration time, getting the consultation, type of investigation done, promptness in giving the investigation report, etc. and the number of possible reasons of the delay. The observations for subjective assessment were collected through field visits and to see directly outpatient service an arrival pattern of patients in OPD of FEHJ.

5. CONCLUSIONS

The results of the study are obtained by addressing each objective as follows.

5.1 The Complete Process Flow of the OPD

The first point of contact between the patient and the hospital staff is OPD, which acts like a mirror reflecting the functioning of the hospital operations. Patients visit OPD for variety of purpose like, consultation, day care treatment; investigation, referral, admission, and post-discharge follow-ups which generate the first impression of the hospital service operations. The process flow at Fortis Escorts Hospital OPD is shown in **Figure 1** given below.

OPD is a critical process for any hospital and analysis of OPD helps to not only identify but also eliminate unnecessary movements for efficient and effective patient care. Assessment of the OPD layout can lead to a reduction in overcrowding and consultation delay which drastically decreases the efforts, patients need for treatment and/or routine check-ups. A more detailed process analysis of the OPD can be seen in **Figure 2** given below.

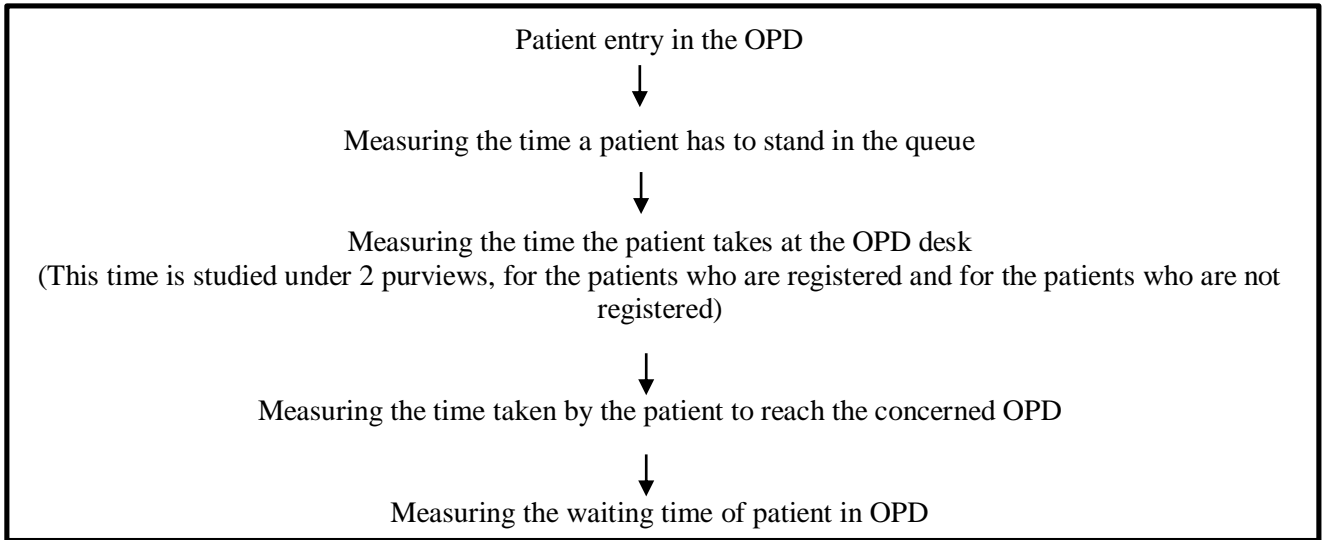


Figure 1 Process flow of fortis escorts hospital OPD

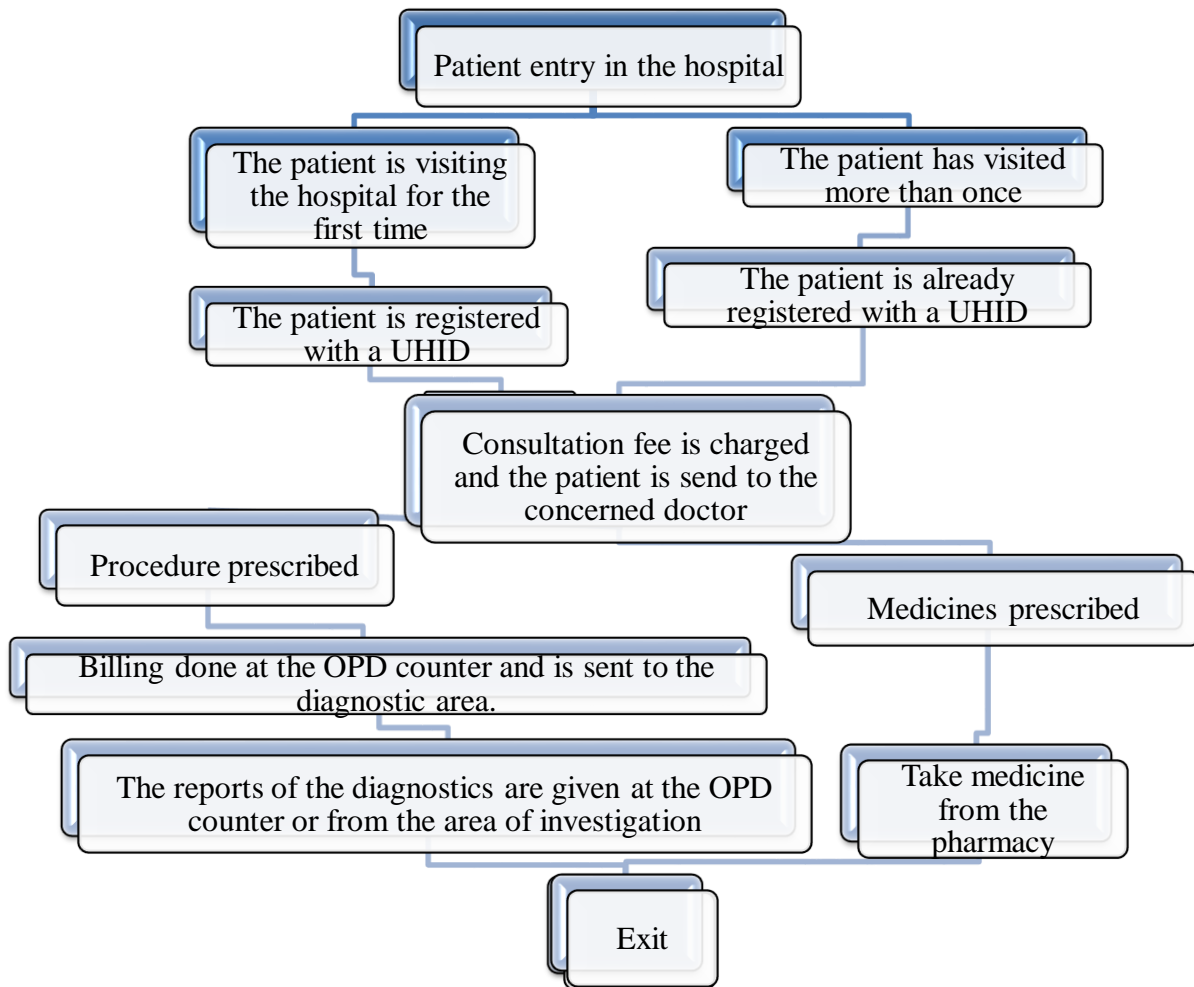


Figure 2 Process analysis of fortis escorts hospital OPD

5.2 Areas Where Patient's Time is Consumed

After understanding the process flow of the outpatient department, there is a need to have a holistic view of OPD at Fortis Escorts Hospital Jaipur. The SWOT analysis is an appropriate method for identifying and assessing the strengths and weaknesses, opportunities and threats in order to optimize the development opportunities of hospital operations. Although SWOT analysis is intended for other industries, it is increasingly important for the healthcare sector, especially in hospital operations. SWOT analysis combines the findings of strategic analysis of the external and internal factors that stimulate the successful operations of the OPD at Fortis Escorts Hospital Jaipur (FEHJ).

Factors which influence strength for OPD at FEHJ are its strategic location of the reception area, well-placed stations all around the area, knowledgeable and trained staff responding to patients need, etc. However, despite that there are still few but relevant weaknesses such as queuing issues at the registration counter of OPD due to non-availability of forms, registered and non-registered patients forming the same queue, less sitting capacity, etc. These factors possess threats for hospital operations at OPD in terms of time constraints for patients leading to lower satisfaction but also provide opportunities for better management of the queues in OPD at FEHJ. The results of the SWOT analysis of OPD at Fortis Escorts Hospital, Jaipur are presented in **Figure 3** given below.



Figure 3 SWOT analysis of OPD at fortis escorts hospital, Jaipur

Table 1 Areas where patient time is wasted

S. No	Problem area identified	Average wait time (minutes)	Projection of time which can be saved
1	Lack of a proper system for informing first-time visitors about registration	9.86	43.86%
2	Delay due to technical errors such as the problem with printers, etc.	2	11.12%
3	Delay due to receptionist taking appointments on the phone	0.5	3.87 %

An objective assessment of 50 patients was done by observing how much time the patients waited in the queue, the time spent by patients at the registration counter, the waiting time in the OPDs for consultation, etc. The study reveals the average waiting time spent by the patients at different OPD and expresses their view towards the hospital service operations. The study also sheds light on the total time consumed by different OPDs.

Pareto's 80:20 Principle, which is a law applicable to all fields of study, states that only 20% of the reasons generate 80% delay in operations. Hence, it is necessary to focus on those critical and few reasons rather than diverting attention towards 80% trivial issues. A retrospective analysis in consultation with doctors for delays in OPD of hospital operation helped in identifying major reasons for delay and recommendations were provided to reduce the waiting time of patients in OPD.

Following Pareto's principal, few critical areas as shown in **Table 1**, were identified which caused delay and addressing these issues could possibly save more than half of patients waiting time.

5.3 Patient's Perception of Delay in OPD

Patients arriving in the OPDs of hospitals are responsible for spreading the good image of the hospital and therefore patient satisfaction is equally important for hospital management. Due to continuous changes in hospital operations, it is difficult to maintain patients' satisfaction as a top priority for OPD which is the first interaction for hospital management. An OPD is a place where non-emergent ambulatory medical care is provided under the supervision of a physician and the attitude of health care providers has its own impact on the satisfaction level of patients. More the positive attitude more the patient is satisfied, patient satisfaction also depends on 'nursing care' because nurses are involved in almost every aspect of patient care in hospital operations.

In this study, it has been observed that 80% of patients rated their level of satisfaction at OPD as Good, 6% patients were dissatisfied with the services at OPD and remaining 14% patients felt average level of satisfaction at OPD. While conducting this study, we found health services make hospital operations more sensitive and alert to patient needs. Many instances in which patients were eager about the services they had received in the hope that some action would be taken determining their level of satisfaction.

5.4 Time Study on Different OPD Stations

OPD indicators related to services in hospital operations are described as follows. The outpatient department is open from 9.00 a.m. till 5.00 p.m. working a total of 9 hours per day. It must be noted that for the purpose of this study, the emergency department which remains open even after 5.00 p.m. is not included. The patient arrival rate each day at OPD is calculated by dividing the average patients per day i.e. 288 by 9 hours of work resulting 32 patients per hour. The service rate of patients was calculated after interviewing with the doctors, one doctor averagely takes 8 minutes to treat one patient which implies that a doctor can see 7 patients per hour.

The registration time is the time consumed at the registration desk and the registration turnaround time (TAT) is the time from when the patient enters OPD until the patient was registered. Patient flow at different OPD with average waiting time can be seen in **Table 2** and the registration TAT came out to be 12 minutes out of which the average registration time was 3 minutes, so we decided to find out the results for OPD 2 without registration using the mean inter-arrival time as 9 minutes. The waiting time hugely depends upon the flow of patients in different OPDs and thus the average waiting time of patients before seeing a doctor was calculated OPD wise.

Table 2 Average waiting time in different OPDs

S. No	OPD	Percentage (%) of patient flow	The average time is taken before seeing a doctor (Minutes)
1	Cardiac OPD	66.66%	16
2	OPD2	19.62%	61
3	OPD1	7.84%	9
4	Paediatric OPD	5.88%	7.5

Source: Fortis escorts hospital, Jaipur

5.5 The Waiting Time of Patients in Different OPD Stations

There is always random arrival of patients for receiving healthcare services and that require immediate availability of service, but they should be able to wait in line with patience when the hospital services are operating at peak capacity. Due to the dynamic nature of hospital service operations, it is often difficult to predict the arrival of no. of patients and time taken for consultation at any given moment.

The goal of the queuing theory is to reach an optimal equilibrium between the arrival rate and service rate of patients in OPD for the smooth functioning of hospital operations. The input parameters for queuing model M/M/1, given in Table 3 are calculated using a number of patients in the system denoted by n, average arrival rate i.e. no. of arrivals per hour denoted by λ and average service rate per server denoted by μ . The symbols and formulae to be used are given in Table 4.

While using queuing model, only 3 OPDs with the highest patient flow i.e. Cardiac, OPD, and OPD2 were considered, comparing the number in queue, waiting time of patients in the queue, waiting time of patients in the system and number in the system all calculated using queuing formulae for modeling. The mean inter-arrival time is exponentially distributed whereas service time of different OPDs is uniformly distributed, hence average is considered

for sensitivity analysis of different OPDs as shown in Table 5.

Table 3 Input parameters for queuing model

Parameter M/M/1 (exponential service times)	Value
Arrival rate (λ)	32 patients per hour
Service rate (μ)	8 patients per hour
No. of OPDs	OPD1, OPD2, Cardiac OPD and Paediatric OPD

Table 4 Symbols and formulae to be used in the calculation of M/M/1 Model

Symbol	Meaning	Formulae in M/M/1 model
P	Operation rate	$\rho = \lambda / \mu$
Wq	Average waiting time in a queue	$Wq = \rho / \mu - \lambda$
Ws	Average entire time in a system	$Ws = 1 / \mu - \lambda$
Lq	Average number of patients in a queue	$Lq = \rho \lambda / \mu - \lambda$
Ls	Average number of patients in a system	$Ls = \lambda / \mu - \lambda$

Table 5 Sensitivity analysis of different OPDs

OPD	Mean inter-arrival time (minutes)	Service time (minutes)	Number in the queue Lq	Wait in the queue Wq (minutes)	Wait in the system Ws (minutes)	Number in the system L
Cardiac	10	8	1.608	16.08	24.08	2.408
OPD I	12	11	5.045	60.54	71.54	5.961
OPD II	8	6	1.135	9.08	15.08	1.885
OPD II with registration	9	7	1.384	12.45	19.45	2.161

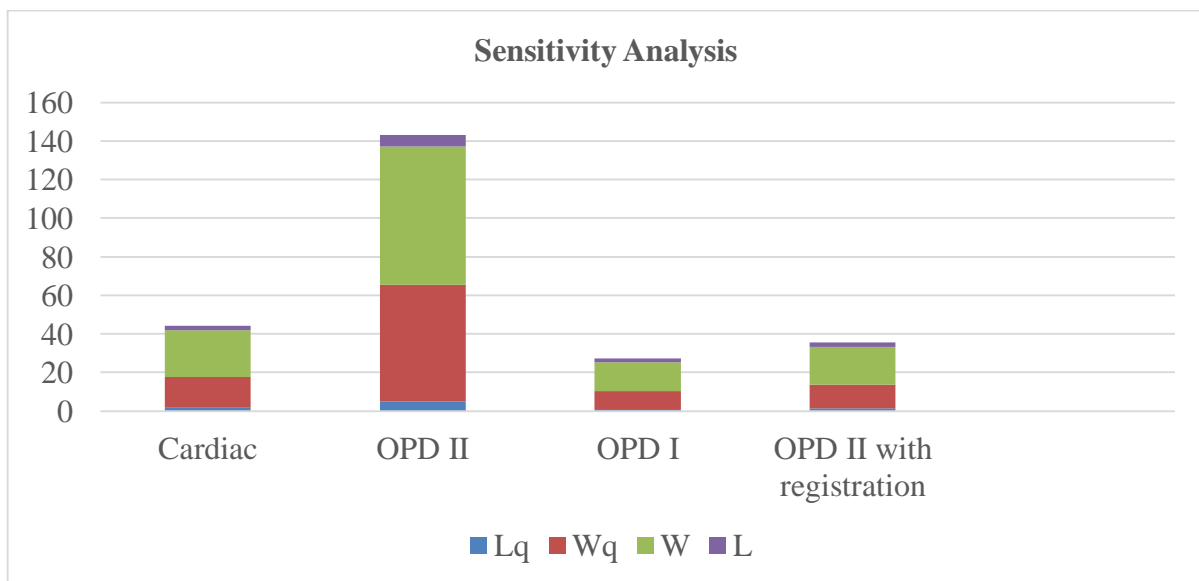


Figure 4 Graphical plot of results of sensitivity analysis

From the results of the sensitivity analysis seen in **Figure 4**, OPD II without registration produces inferior performance compared to other OPDs. OPD I provide the optimal performance along with cardiac OPD and the change in time spent in the queue as we move from OPD II without registration to OPD II with registration is very appreciable. In addition, authentication of the results obtained was conducted by cross-checking the time registration system of OPD II wherein the waiting time in the system of OPD II post registration was calculated manually according to the flow of patients. It was found with 95% accuracy that waiting time according to our study was 19.45 minutes and manually calculated waiting time according to patient flow came out to be 20.6 minutes.

Based on the results obtained, it is found that first, the hospital lacks in having a proper system for letting patients know about registration especially the first-time visitors. There is wastage of time for the patient or their relatives in figuring out the exact procedures for the registration of new patients. Secondly, there were some minor technical errors such as improper placement of the registration form in the OPD main lobby, printer problem, etc. which added to the queuing challenge at OPD. Lastly, the signage indicating the counters for new registration, old registration, and golden age club patients were hanged little too high which makes it difficult for patients entering the hospital to read the signage and choose the queue accordingly which later created confusion and delayed the process. However, given the size and scale of the multi-specialty hospital, these were just a few indicators giving scope for improvement in the future.

6. CONCLUSIONS, RECOMMENDATIONS, AND LIMITATIONS

First and foremost, it is necessary to prioritize hospital operations according to the need, benefit and feasibility since the OPD coordinators find it difficult to keep track of patients, especially on Mondays, Thursdays, and Saturdays when there is high footfall. The registration forms must be placed near the new registration counter which should be made noticeable by bringing the signage a little down. Due to place constraints, not more than 2 attendants should be allowed per patient and guidance must be provided to the same for procedures expected as soon as the patient enters the main lobby. Queue managers can help in separating the patients into old and new and make sure no appointment is scheduled at the time of clinical rounds of consultants. The perceived waiting time can be reduced by providing facilities such as proper sitting arrangements, putting a TV, air conditioners, etc.

The most crucial element in increasing patient satisfaction in hospital operations is timely access i.e. "When" care is provided followed by "What" care is given. Waiting time plays a very crucial role in healthcare business and this study demonstrates the analysis and application of queuing theory in hospital operations for the improvement of process efficiency of OPDs. Patients' dissatisfaction associated with long waiting queues is well-known and the perceived waiting is much more annoying for the patients than the actual waiting time. The study has revealed that the subjective waiting time is highly co-related with the

frustration of the patient than the objective waiting time. It is highly recommended to replicate the study in OPDs of other hospitals to verify the effectiveness of queuing theory for addressing queuing challenges faced by hospital operations in India.

Research focusing on the relative impact of word of mouth communication, personal needs and past experience on patients' service expectations in hospital operations within as well as across service categories can have useful managerial implications. Empirical research aimed at ascertaining whether, and in what ways patients service expectations differ will be valuable from a service marketers' viewpoint with regards to hospital operations and healthcare industry in general. The major insights gained through this study will hopefully spawn both academic and practitioner's interest in using queuing theory for service quality determination in hospital operations.

The morbidity pattern and thus the footfall may vary during the period of study since it was done for a confined time period. The emergency counter which also deals with the outpatients was not included in the study as there are patients of critical nature and they serve on a first come, first serve basis. In addition, in-depth interviews of the patients would have yielded a better understanding but due to time constraints and also considering the restless conditions of the patients it was deliberately avoided.

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